

WHEN PERFORMING SOME COMPUTATIONS RELATED TO ARCFUNCTIONS

$f(x) = \arctg 1 + \arctg\left(1 + \frac{1}{x}\right) + \arctg(1 + 2x)$ APPLICATIONS OF THE FUNCTION VALUE FIELD

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ANNOTATION

In this article $f(x) = \arctg 1 + \arctg\left(1 + \frac{1}{x}\right) + \arctg(1 + 2x)$ theoretical information is provided about performing some calculations related to arcfuntions by applying the field of function values, and the necessary examples are solved.

First of all $f(x) = \arctg 1 + \arctg\left(1 + \frac{1}{x}\right) + \arctg(1 + 2x)$ we find the area of values of the function.

The domain of definition of this function is all real numbers other than zero

$$D(f) = (-\infty; 0) \cup (0; \infty)$$

$f(x)$ value domain of the function $E(f)$ let's consider 5 cases of finding.

$$1) \begin{cases} 1 + \frac{1}{x} < 0 \\ 1 + 2x < 0 \end{cases}$$

In this case $-1 < x < -\frac{1}{2}$ and $A(x) < 0$, in this $A(x) = \arctg\left(1 + \frac{1}{x}\right) + \arctg(1 + 2x)$

$$\operatorname{tg} A(x) = \frac{1 + \frac{1}{x} + 1 + 2x}{1 - \left(1 + \frac{1}{x}\right)(1 + 2x)} = \frac{2 + 2x + \frac{1}{x}}{-2 - 2x - \frac{1}{x}} = -1.$$

$2 + 2x + \frac{1}{x} < 0$ since $\left(-1; -\frac{1}{2}\right)$ all in the range x for lar

$$A(x) = -\frac{\pi}{4}; \quad f(x) = \arctg 1 + A(x) = \frac{\pi}{4} - \frac{\pi}{4} = 0$$

$$2) \begin{cases} 1 + \frac{1}{x} < 0 \\ 1 + 2x > 0 \end{cases}$$

In this case $-\frac{1}{2} < x < 0$ and $B(x) > 0$ in this $B(x) = \arctg 1 + \arctg(1 + 2x)$.

$$\operatorname{tg} B(x) = \frac{1 + 1 + 2x}{1 - 1 + (1 + 2x)} = \frac{2 + 2x}{-2x} = -\left(1 + \frac{1}{x}\right)$$

and

$$B(x) = -\arctg\left(1 + \frac{1}{x}\right).$$

So $f(x)=\arctg(1+\frac{1}{x})+B(x) = \arctg(1+\frac{1}{x}) \cdot \arctg(1+\frac{1}{x})=0$

$$3) \begin{cases} 1+\frac{1}{x} > 0 \\ 1+2x < 0 \end{cases}$$

In this $x < -1$ va $C(x) > 0$, in this $C(x) = \arctg 1 + \arctg\left(1+\frac{1}{x}\right)$

$$\operatorname{tg}C(x) = \frac{1+1+\frac{1}{x}}{1-1\cdot\left(1+\frac{1}{x}\right)} = \frac{2+\frac{1}{x}}{-\frac{1}{x}} = -(1+2x)$$

$$\operatorname{tg}C(x) = -\arctg(1+2x).$$

So, $f(x) = C(x) + \arctg(1+2x) = -\arctg(1+2x) + \arctg(1+2x) = 0$

$$4) f(-1) = \arctg 1 + \arctg\left(1+\frac{1}{-1}\right) + \arctg(1+2(-1)) = 0.$$

$$f\left(-\frac{1}{2}\right) = \arctg 1 + \arctg\left(1+\frac{1}{-\frac{1}{2}}\right) + \arctg\left(1+2\cdot\left(-\frac{1}{2}\right)\right) = 0$$

So $x < 0$ da $f(x) = 0$.

$$5) \begin{cases} 1+\frac{1}{x} > 0 \\ 1+2x > 0 \end{cases}$$

$$D(x) = \arctg\left(1+\frac{1}{x}\right) + \arctg(1+2x),$$

$$\operatorname{tg}D(x) = \frac{1+\frac{1}{x}+1+2x}{1-\left(1+\frac{1}{x}\right)(1+2x)} = \frac{2+2x+\frac{1}{x}}{-2-2x-\frac{1}{x}} = -1.$$

$(0;+\infty)$ in the range x for all values of

$$2+2x+\frac{1}{x} > 0$$

$$D(x) = \frac{3\pi}{4}; \quad f(x) = \arctg 1 + D(x) = \frac{\pi}{4} + \frac{3\pi}{4} = \pi.$$

So, $x > 0$ da $f(x) = \pi$.

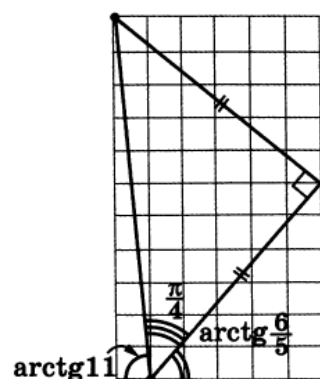
Now it is not difficult to find the area of values of a given function.

$$E(f) = \{0; \pi\}$$

Example. $f(5)$ we find the value of in 3 different ways.

Method 1. $5 > 0$ since $\operatorname{uch} 1 \ln \quad f(5) = \arctg 1 + \arctg \frac{6}{5} + \arctg 1 = \pi$.

Method 2. Look at the drawing.



Method 3. $\arctg 1 = \frac{\pi}{4}$; $\arctg 1 > 0$, $\arctg \frac{6}{5} > 0$.

$$\operatorname{tg}(\arctg 1 + \arctg 1) = \frac{1+11}{1-1 \cdot 11} = -\frac{6}{5}.$$

So

$$\arctg 1 + \arctg 1 = \pi - \arctg \frac{6}{5}$$

and

$$f(5) = \arctg \frac{6}{5} + \pi - \arctg \frac{6}{5} = \pi$$

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